**Dynamic Programming**

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# **Theory**

## What is Dynamic Programming?

Dynamic programming (DP) is an optimization technique used to solve complex problems by breaking them down into simpler subproblems and storing the results of these subproblems to avoid redundant computations. It is particularly useful for problems with overlapping subproblems and optimal substructure properties.

**Key Concepts of Dynamic Programming:**

1. **Overlapping Subproblems**: Solving the same subproblems multiple times.
2. **Optimal Substructure**: The optimal solution to a problem can be constructed from optimal solutions of its subproblems.
3. **Memoization**: Storing results of subproblems to reuse them, thus saving computation time. Also called top-down approach.
4. **Tabulation**: Building a table in a bottom-up manner to store solutions of subproblems.

**Steps to approach Dynamic Programming problems:**

1. Find the recurrence relationship
2. Find the base case
3. Find way to store solutions of subproblems

# **Sample Code**

## Fibonacci Series – Recursion:

def fib(n):

    if n<=1:

        return n

    else:

        return fib(n-1) + fib(n-2)

# fib : 0,1,1,2,3,5,8

print(fib(6)) #8

Here we see, our solution finding solution of same subproblems several time, which cause slowness. We can prevent this using DP, by saving solution of subproblems in an array.

## Fibonacci Series –Top down:

Here we built solution from n to i, normally via recursion.

def fib\_top\_down(n, dp):

    if n<=1:

        return n

    if dp[n]!= -1:

        return dp[n]

    else:

        dp[n]= fib\_top\_down(n-1, dp) + fib\_top\_down(n-2, dp)

        return dp[n]

n=6

dp = [-1]\*(n+1)

print(fib\_top\_down(n, dp)) #8

## Fibonacci Series – Bottom Up:

Here we built solution from i to n, normally via loop.

def fib\_bottom\_up(n):

    dp = [-1]\*(n+1)

    dp[0], dp[1] = 0, 1

    for i in range(2,n+1):

        dp[i] = dp[i-1] + dp[i-2]

    return dp[n]

print(fib\_bottom\_up(6)) #8

## Fibonacci Series – Bottom Up – Space Optimized:

In place of dp array we can use 2 variables for same purpose

def fib\_bottom\_up(n):

    prev = 1

    prev1 = 0

    curr = 0

    for i in range(2,n+1):

        curr = prev + prev1

        prev1 = prev

        prev = curr

    return prev

print(fib\_bottom\_up(6)) #8

# LEVEL 1: **EASY**

### Climbing Stairs

Link: <https://leetcode.com/problems/climbing-stairs/description/>

1. You are given money present in n adjacent houses, there is robber who wants to rob the houses. But he cannot rob from 2 adjacent houses. Find max loot of robber.

### Min cost climbing stairs

Link: <https://leetcode.com/problems/min-cost-climbing-stairs/>

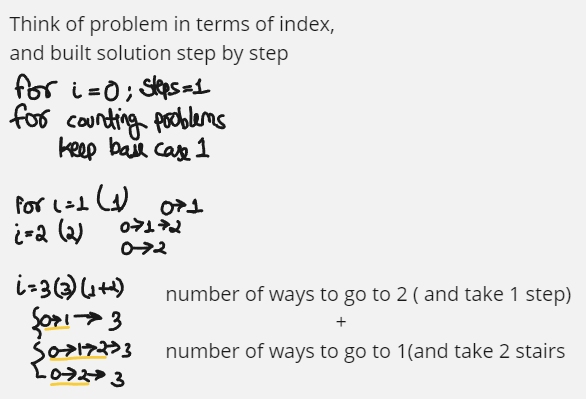
# LEVEL 2: **Medium**

# LEVEL 3: **Difficult**

# **SOLUTIONS:**

## **LEVEL 1:**

1. Climbing Stairs



# for n = number of ways to go to n-1 + number of ways to go to n-2

# 0->1 for making code easy

# 1->1

# 2 -> 2  (0->2 , 0->1->2)

class Solution:

    def climbStairs(self, n: int) -> int:

        dp = [1]\*(n+1)

        for i in range(2,n+1):

            dp[i] = dp[i-1] + dp[i-2]

        return dp[n]

class Solution:

    def climbStairs(self, n: int) -> int:

        def helper(n):

            if n==0: return 1

            if n==1: return 1

            if dp[n]!=-1 : return dp[n]

            dp[n] = helper(n-1) + helper(n-2)

            return dp[n]

        dp = [-1]\*(n+1)

        return helper(n)

1. Loot house

F[i] = max loot done till ith house, so F[i] = max ( arr[i] + F[i-2] , F[i-1] )

*#Loot HOUSE*

def lootBU(n,arr):

    dp=[0]\*(n)

    dp[0],dp[1] = arr[0],max(arr[0],arr[1])

    for i in range(2,n):

        dp[i] = max(arr[i]+dp[i-2] ,dp[i-1])

    print(dp)

    return dp[n-1]

arr = [6,2,3,9]

print(lootBU(len(arr),arr))

1. Min cost climbing stairs

Here dp[i] = cost of reaching at ith step.

#Bottom-up

class Solution:

    def minCostClimbingStairs(self, cost: List[int]) -> int:

        dp = [0]\*len(cost)

        dp[0] = cost[0]

        dp[1] = cost[1]

        for i in range(2,len(cost)):

            dp[i] = cost[i]+min(dp[i-1],dp[i-2])

        return min(dp[-1],dp[-2])

#Top-down

class Solution:

    def minCostClimbingStairs(self, cost: List[int]) -> int:

        n=len(cost)

        self.dp = [-1]\*n

        self.dp[0]=cost[0]

        self.dp[1]=cost[1]

        def helper(n):

            if self.dp[n]!=-1:

                return self.dp[n]

            else:

                self.dp[n] = cost[n] + min(helper(n-1),helper(n-2))

                return self.dp[n]

        helper(n-1)

        return min(self.dp[-1],self.dp[-2])